

Q4 (2016):

$$\begin{aligned} \text{2. } \log p(x, c | \mu, \pi) &= \sum_{i=1}^N \log p(x_i, c_i | \mu, \pi) \\ &= \sum_{i=1}^N \left[\delta(c_i = H) \left[\log \mu + \delta(x_i = HH) \log (\pi^2) + \delta(x_i = HT) \log (\pi(1-\pi)) + \right. \right. \\ &\quad \left. \left. \delta(x_i = TH) \log ((1-\pi)\pi) + \delta(x_i = TT) \log (1-\pi)^2 \right] + \right. \\ &\quad \left. \delta(c_i = T) \left[\log(1-\mu) + \delta(x_i = HH) \log \pi + \delta(x_i = TT) \log (1-\pi) + \right. \right. \\ &\quad \left. \left. \delta(x_i = HT) \log 0 + \delta(x_i = TH) \log 0 \right] \leftarrow (\text{optional}) \right] \end{aligned}$$

$F(q, \mu, \pi) \rightarrow$ (replace $\delta(c_i = H)$ with q_i & $\delta(c_i = T)$ with $(1-q_i)$ above.)